

# How to use `polyline.m`?

- Define an inner function `[fout,gout]=f(x)` where `fout=f(x)` is a scalar and `gout = grad f(x)` is a COLUMN vector
- Ex: for this homework

```
function [z g]= f(x)
    z = (1-x(1))^2+100*(x(2)-x(1)^2)^2;
    g = [400*x(1)^3+2*x(1)-400*x(1)*x(2)-2
         200*x(2)-200*x(1)^2];
end
```

# How to use `polyline.m`?

- When calling `polyline`,

```
[x idid] = polyline(x, fk, gk, pk, ft, @f, 10);  
if(idid == -1) % error handling
```

- `x`, `gk`, `pk` are vectors; `fk`, `ft` are scalar

- $ft = f(x + \alpha_0 * pk)$ .

- You can set  $\alpha_0 = 1$  or other value  $0 < \alpha_0 < 1$ . See some difference results.

- If you use  $\alpha_0 = \min(1, 1/(1 + \text{norm}(gout)))$ , you need to explain how it is derived and why it works.

# What does `polymod.m` do?

- Use the interpolation method to find  $\min \phi(\alpha) = f(x + \alpha p)$  in the interval  $[0, \text{lamc}]$ .
  - More precisely, in  $[\text{blow} * \text{lamc}, \text{bhigh} * \text{lamc}]$
- In the first step, we have  $\phi(0)$ ,  $\phi'(0)$ ,  $\phi(\text{lamc}) = q_c$ 
  - Use quadratic model to find the minimum.
  - Note that **lamc=1 in polyline.m**
  - So the model function  $q(\alpha)$  is
$$q(\alpha) = (q_c - q_0 - qp_0)\alpha^2 + qp_0\alpha + q_0$$
  - whose extremum is at  $\alpha = -qp_0 / 2(q_c - q_0 - qp_0)$

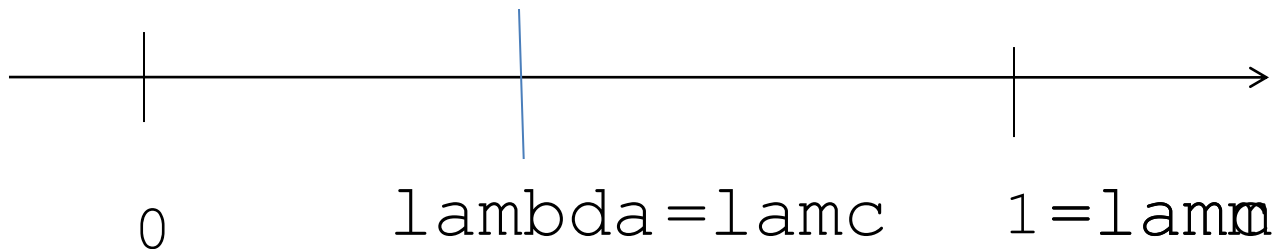
# The quadratic model

- But the extremum  $l_{plus}$  may not be in the interval  $l = [b_{low} * \lambda_{mc}, b_{high} * \lambda_{mc}]$ 
  - The minimum value is on the boundary

```
lleft=lamc*blow; lright=lamc*bhigh;
% quadratic model
% q(0) = q0, q'(0) = qp0, q(lamc) = qc
lplus = -qp0 / (2 * lamc * (qc - q0 - qp0));
if lplus < lleft lplus = lleft; end
if lplus > lright lplus = lright; end
```

# After the first iteration

- we have a new point  $\lambda$
- additional info  $f(\lambda)$ ,
  - $\lambda$  is got from previous iteration. ( $=\lambda_{old}$ )
  - Use cubic model to find the minimum



# The cubic model

```
% cubic model
% q(0) = q0, q'(0) = qp0, q(lamc) = qc,
q(lamm) = qm
a=[lamc^2, lamc^3; lamm^2, lamm^3];
b=[qc; qm] - [q0+qp0*lamc; q0+qp0*lamm];
c=a\b;
lplus=(-c(1)+sqrt(c(1)*c(1)-
3*c(2)*qp0))/(3*c(2));
if lplus < lleft lplus = lleft; end
if lplus > lright lplus = lright; end
```

- It's the homework to figure out what those statements do.